

Experiment Solution

A2

English



Q2 Exploring the spatial structure of the sample with optical methods

Solution

Part A. Collimation of light and sample

A.1

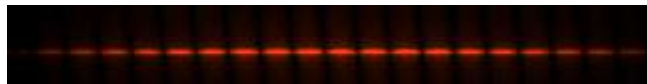
0.5 pt

$$(X_{\text{sample}}, Y_{\text{sample}}) = \underline{\underline{(3700, -2900)}}$$

A.2

0.5 pt

Interference pattern:



Order, fringe	-2, Dark	-1, Dark	1, Dark	2, Dark
(x, y)	(-0.98, 0)	(-0.38, 0)	(0.34, 0)	(0.98, 0)
S (cm)	0.98	0.38	0.34	0.98
ΔS (cm)	0.65			

Part B. Exploration of sample structure size

B.1

0.5 pt

$$d = \frac{m \times \lambda}{\sin\left(\tan^{-1}\left(\frac{S}{L}\right)\right)}$$

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B.2

1.5 pt

$$L = \underline{\underline{60 \text{ cm}}}$$

$$\lambda = \underline{\underline{488 \text{ nm}}}$$

Data	1	2	3	4	5
(x, y)	(-4.04, 4.68)	(3.00, 5.50)	(4.08, -4.60)	(5.76, 0.48)	(-5.68, 0.56)
S (cm)	6.18	6.26	6.15	5.78	5.71
\bar{S} (cm)	6.02 ± 0.11				
$\tan^{-1}\left(\frac{\bar{S}}{L}\right)$	0.0999 ± 0.0019				

$$\lambda = \underline{\underline{514 \text{ nm}}}$$

Data	1	2	3	4	5
(x, y)	(3.32, 5.64)	(6.16, 0.48)	(4.46, -4.90)	(-3.12, -5.64)	(-6, -0.64)
S (cm)	6.54	6.18	6.63	6.45	6.03
\bar{S} (cm)	6.37 ± 0.11				
$\tan^{-1}\left(\frac{\bar{S}}{L}\right)$	0.1057 ± 0.0019				

$$\lambda = \underline{\underline{632.8 \text{ nm}}}$$

Data	1	2	3	4	5
(x, y)	(4.04, 7.00)	(7.44, 0.68)	(5.24, -5.96)	(-3.96, -7.04)	(-7.44, -0.68)
S (cm)	8.08	7.47	7.94	8.08	7.47
\bar{S} (cm)	7.81 ± 0.14				
$\tan^{-1}\left(\frac{\bar{S}}{L}\right)$	0.1294 ± 0.0023				

$$\lambda = \underline{\underline{694.3 \text{ nm}}}$$

Data	1	2	3	4	5
(x, y)	(-5.84, 6.50)	(8.20, 0.76)	(-4.28, -7.72)	(5.96, -6.60)	(4.48, 7.72)
S (cm)	8.74	8.24	8.83	8.89	8.93

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\bar{S} (cm)	8.73 ± 0.13
$\tan^{-1}\left(\frac{\bar{S}}{L}\right)$	0.1444 ± 0.0021

B.3

1.0 pt

$$a = 5.627 \mu\text{m}$$

λ (nm)	d (μm)	a (μm)
488	4.89	5.65
514	4.87	5.63
632.8	4.90	5.66
\bar{a} (μm)	5.627 ± 0.020	

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Part C. Exploration of sample structure size

C.1

0.8 pt

$$\lambda = \underline{488 \text{ nm}}$$

L=90 cm, Axis1				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(3.01, 1.46)	(3.67, 1.91)	(4.30, 2.24)	(5.00, 2.50)
S (cm)	3.35	4.14	4.85	5.59
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0372	0.0459	0.0538	0.0620

L=90 cm, Axis 2				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(-1.64, 3.46)	(-2.07, 4.19)	(-2.41, 4.95)	(-2.87, 5.73)
S (cm)	3.83	4.67	5.51	6.41
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0425	0.0519	0.0611	0.0711

$$\lambda = \underline{514 \text{ nm}}$$

L=90 cm, Axis1				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(3.08, 1.56)	(3.76, 1.92)	(4.44, 2.28)	(5.20, 2.60)
S (cm)	3.45	4.22	4.99	5.81
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0383	0.0469	0.0554	0.0645

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L=90 cm, Axis 2				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(-1.76, 3.68)	(-2.26, 4.38)	(-2.58, 5.34)	(-3.22, 6.04)
S (cm)	4.09	4.92	5.93	6.84
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0454	0.0547	0.0658	0.0759

$\lambda = \underline{\underline{632.8 \text{ nm}}}$

L=90 cm, Axis 1				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(3.84, 1.96)	(4.68, 2.44)	(5.48, 2.88)	(6.44, 3.32)
S (cm)	4.31	5.28	6.19	7.25
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0479	0.0586	0.0687	0.0803

L=90 cm, Axis 2				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(-2.28, 4.56)	(-2.84, 5.48)	(-3.36, 6.52)	(-3.84, 7.52)
S (cm)	5.10	6.17	7.33	8.44
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0566	0.0685	0.0813	0.0935

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English



$$\lambda = \underline{\underline{694.3 \text{ nm}}}$$

L=90 cm, Axis 1				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(4.24, 2.12)	(5.08, 2.80)	(6.04, 3.20)	(7.04, 3.68)
S (cm)	4.74	5.80	6.84	7.96
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0526	0.0644	0.0758	0.0882

L=90 cm, Axis 2				
Order, fringe	4, Bright	5, Bright	6, Bright	7, Bright
(x, y)	(-2.48, 5.00)	(-3.08, 6.04)	(-3.60, 7.16)	(-4.16, 8.28)
S (cm)	5.58	6.78	8.01	9.27
$\tan^{-1}\left(\frac{S}{L}\right)$	0.0619	0.0752	0.0888	0.103

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C.2

0.7 pt

λ (nm)	ΔS_ℓ (cm)	ℓ (μm)	ΔS_w (cm)	w (μm)
488	0.748	58.7	0.860	51.1
	0.750	58.5	0.842	52.1
514	0.787	58.8	0.920	50.3
	0.794	58.3	0.891	51.9
632.8	0.978	58.2	1.12	51.1
	0.960	59.3	1.11	51.4
694.3	1.07	58.2	1.23	50.9
	1.07	58.2	1.22	51.4

$$\ell = 58.59 \mu\text{m}$$

$$w = 50.78 \mu\text{m}$$

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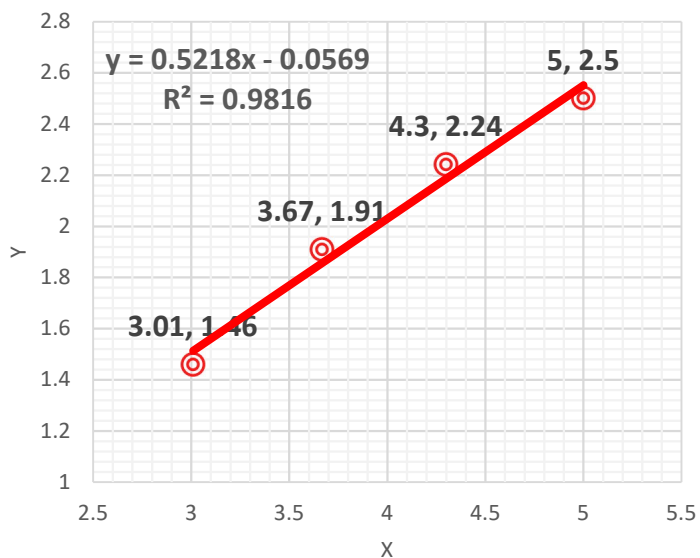
English



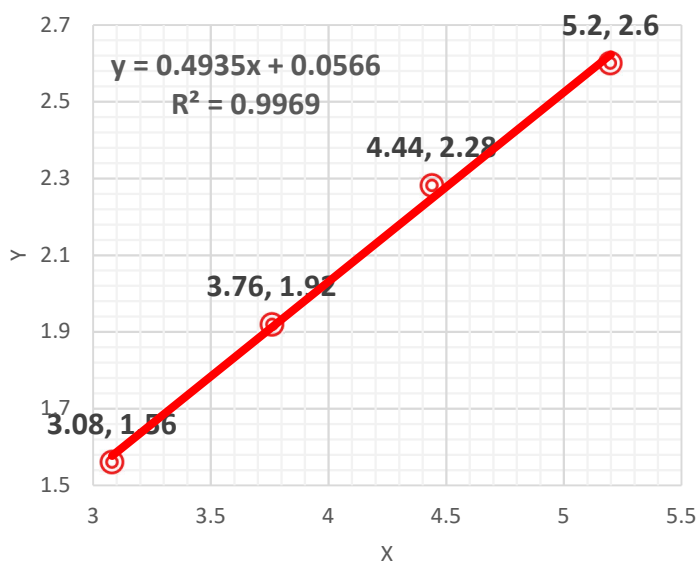
C.3 $\phi = 27^\circ$

1.0 pt

$\lambda =$ 488 nm Axis 1 (long) $\phi =$ 27.6°



$\lambda =$ 514 nm Axis 1 (long) $\phi =$ 26.2°



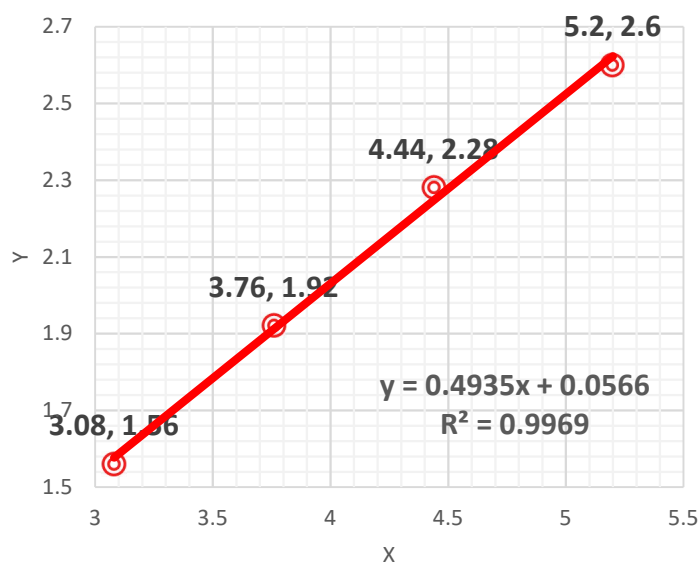
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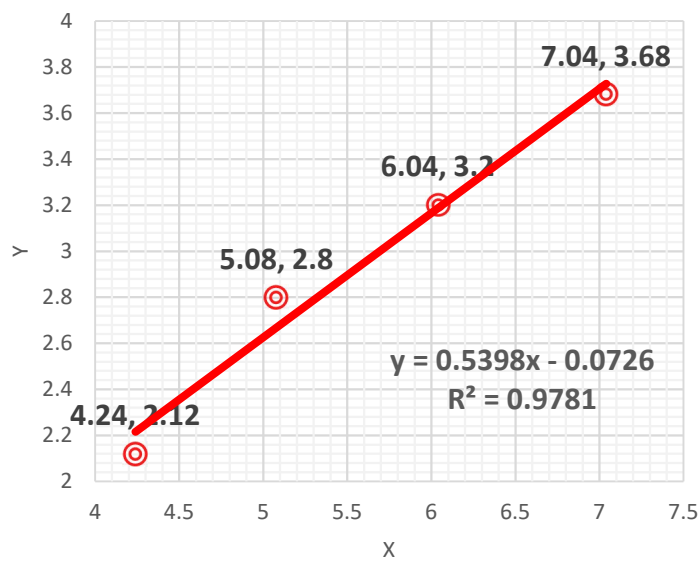
English



$\lambda = \underline{632.8 \text{ nm}}$ Axis 1 (long) $\phi = \underline{27.7}$



$\lambda = \underline{694.3 \text{ nm}}$ Axis 1 (long) $\phi = \underline{28.4}$



Experiment Solution

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Part D. Exploration of sample structure size

D.1

1.9 pt

Laser wavelength $\lambda = \underline{914 \text{ nm}}$

The center coordinates of the fine diffraction bright spot (x, y) long

(1.98, 0.40)	(2.36, 1.62)	(2.64, 1.68)	(3.02, 1.68)
(1.96, 0.82)	(2.32, 1.22)	(2.70, 1.28)	(3.02, 1.30)
(1.98, 1.24)	(2.32, 0.84)	(2.66, 0.84)	(3.04, 1.66)
(1.98, 1.66)	(2.36, 0.42)	(2.62, 0.40)	(2.98, 0.50)

The center coordinates of the fine diffraction bright spot (x, y) short

(-2.06, 3.48)	(-1.72, 3.48)	(-1.38, 3.46)	(-1.06, 3.46)
(-2.08, 3.08)	(-1.74, 3.08)	(-1.40, 3.14)	(-1.00, 3.12)
(-2.08, 2.64)	(-1.74, 2.65)	(-1.38, 2.62)	(-1.02, 2.62)
(-2.06, 2.16)	(-1.68, 2.22)	(-1.36, 2.22)	(-1.02, 2.14)

Calculate the distances between adjacent spots $\Delta S_x \cdot \Delta S_y$

	ΔS_x (cm)	ΔS_y (cm)
long	0.346	0.410
short	0.348	0.428

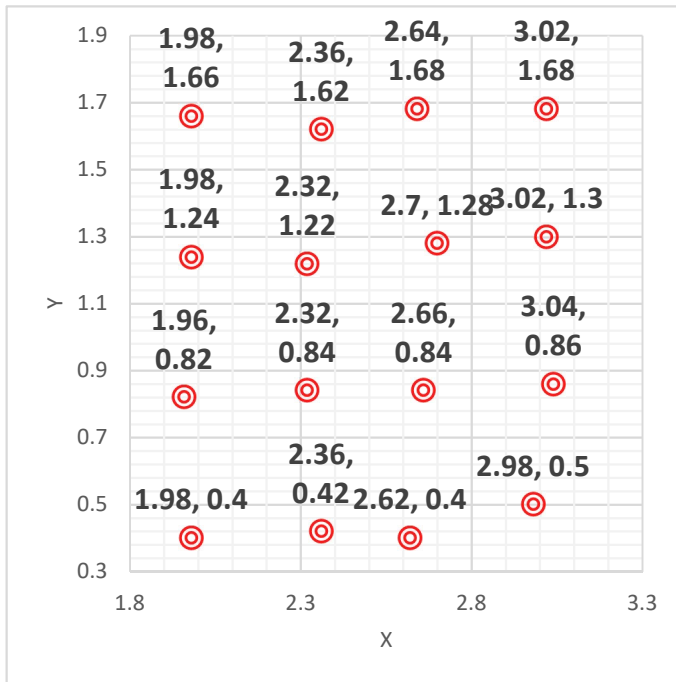
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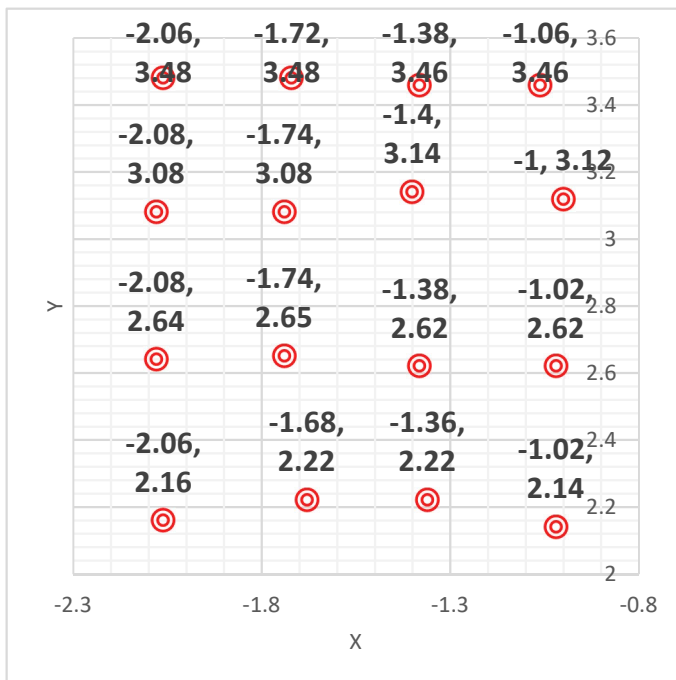
English



D.1.
long



short



Experiment Solution

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English



Laser wavelength $\lambda = \underline{1152 \text{ nm}}$			
The center coordinates of the fine diffraction bright spot (x, y) long			
(2.16, 0.56)	(2.60, 0.56)	(3.04, 0.56)	(3.48, 0.56)
(2.12, 1.16)	(2.58, 1.16)	(3.06, 1.14)	(3.48, 1.12)
(2.12, 1.64)	(2.60, 1.66)	(3.04, 1.68)	(3.48, 1.66)
(2.14, 2.26)	(2.62, 2.22)	(3.08, 2.18)	(3.48, 2.24)
The center coordinates of the fine diffraction bright spot (x, y) short			
(-3.44, 4.44)	(-2.68, 4.42)	(-2.20, 4.42)	(-1.78, 4.42)
(-3.10, 3.86)	(-2.70, 3.88)	(-2.24, 3.84)	(-1.82, 3.88)
(-3.20, 3.38)	(-2.74, 3.38)	(-2.22, 3.34)	(-1.76, 3.34)
(-3.14, 2.78)	(-2.68, 2.78)	(-2.22, 2.78)	(-1.76, 2.76)
	ΔS_x (cm)	ΔS_y (cm)	
long	0.448	0.555	
short	0.452	0.550	

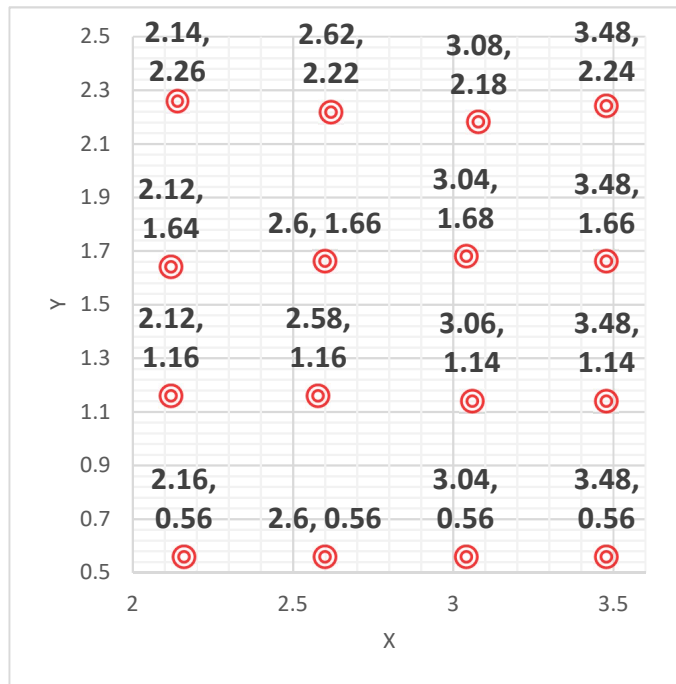
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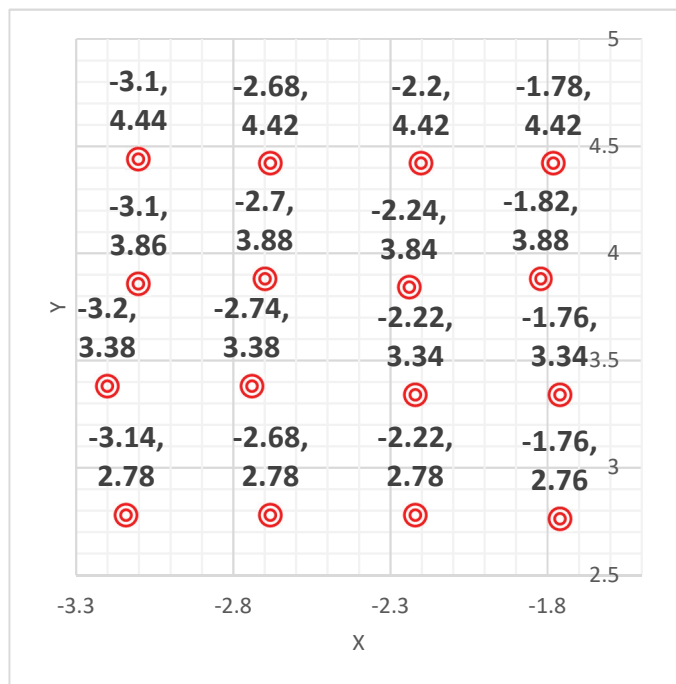
English



long



short



Experiment Solution

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English



Laser wavelength $\lambda =$ <u>1444 nm</u>			
The center coordinates of the fine diffraction bright spot (x, y) long			
(3.34, 0.02)	(3.86, 0.02)	(4.42, 0.02)	(4.94, 0.04)
(3.34, 0.70)	(3.84, 0.72)	(4.42, 0.70)	(4.94, 0.74)
(3.36, 1.42)	(3.86, 1.42)	(4.44, 1.40)	(5.00, 1.46)
(3.34, 2.08)	(3.86, 2.08)	(4.48, 2.08)	(5.00, 2.10)
The center coordinates of the fine diffraction bright spot (x, y) short			
(-3.86, 4.16)	(-3.32, 4.18)	(-2.74, 4.18)	(-2.14, 4.16)
(-3.84, 3.48)	(-3.28, 3.48)	(-2.72, 3.48)	(-2.12, 3.48)
(-3.80, 2.78)	(-3.26, 2.78)	(-2.72, 2.78)	(-2.12, 2.80)
(-3.78, 2.02)	(-3.26, 2.06)	(-2.70, 2.06)	(-2.00, 1.98)
計算圖形斑點間距 ΔS_x 、 ΔS_y 0.5 pt			
	ΔS_x (cm)	ΔS_y (cm)	
long	0.542	0.687	
short	0.575	0.713	

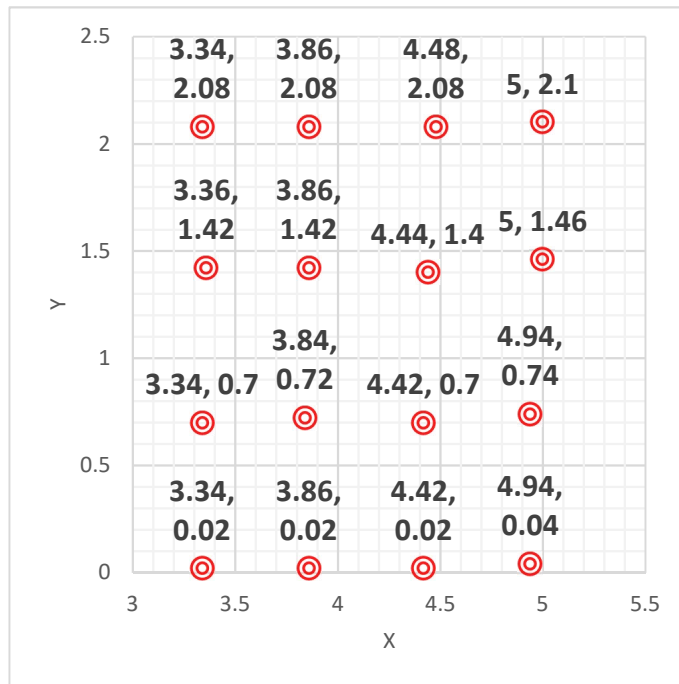
Experiment Solution

A2

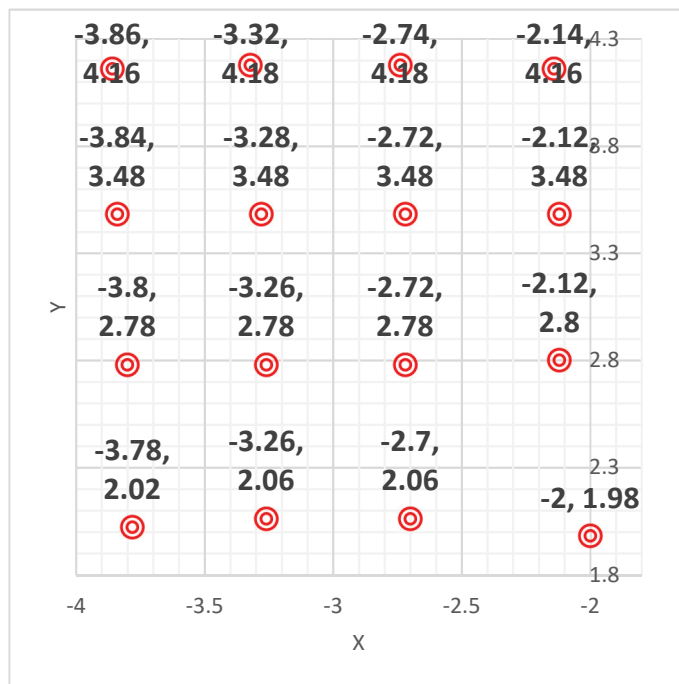
English



long



short



Experiment Solution

A2

English



D.2

0.6 pt

$$d_x = 249.3 \mu\text{m} \quad d_y = 198.2 \mu\text{m}$$

λ (nm)		d_x (μm)	d_y (μm)
914	long Axis	251	211
	short Axis	250	203
1152	long Axis	244	197
	short Axis	242	199
1444	long Axis	253	199
	short Axis	239	192

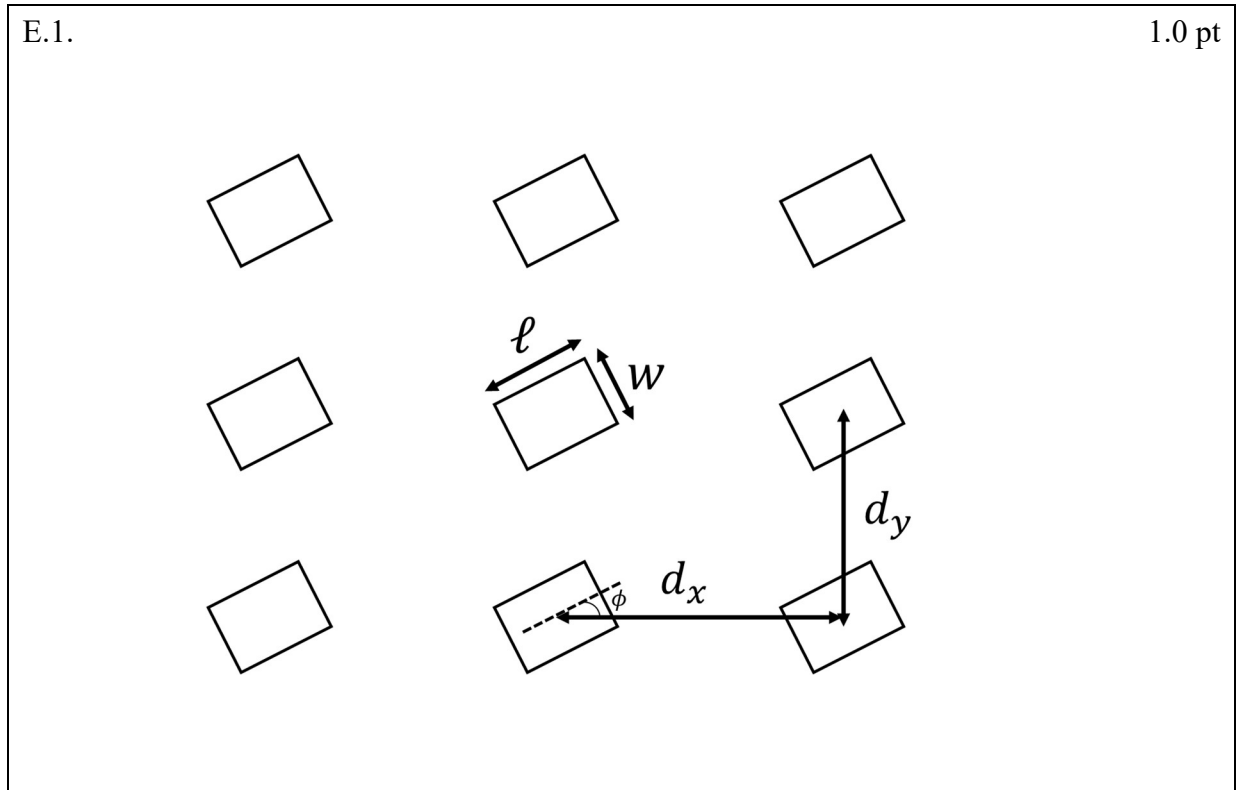
Experiment Solution

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Part E. Exploration of sample structure size



$(a, \ell, w, d_x, d_y, \phi) =$

(5.627 μm , 58.59 μm , 50.78 μm , 249.3 μm , 198.2 μm , 27 degree)